

# Measurement of the $B(E2; 2_1^+ \rightarrow 0_1^+)$ in neutron-rich $^{182}\text{Hf}$

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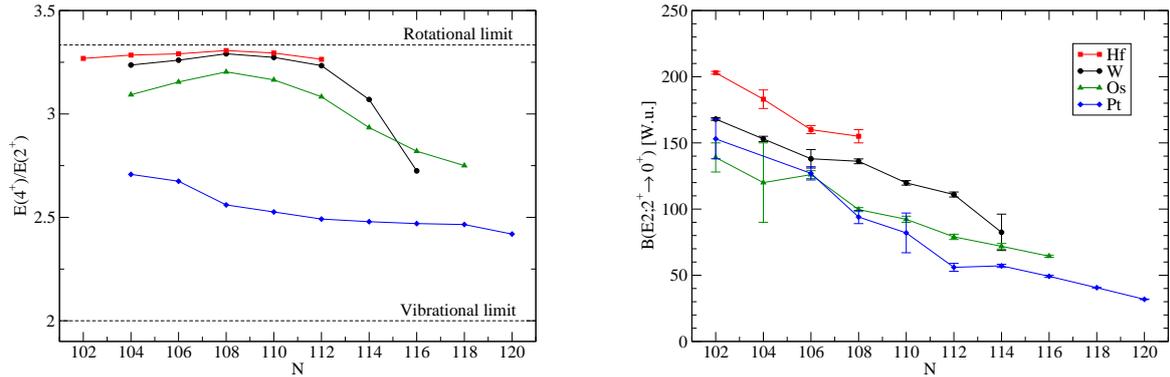
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We propose to measure the half-life of the yrast  $2^+$  state, and thus the  $B(E2; 2_1^+ \rightarrow 0_1^+)$ , in  $^{182}\text{Hf}$ . The  $^{180}\text{Hf}(^7\text{Li}, \alpha\text{p})^{182}\text{Hf}$  incomplete-fusion/transfer reaction will be used to populate excited states in  $^{182}\text{Hf}$  and  $\gamma$  rays will be detected in the ROSPHERE array of high-purity germanium (HPGe) and lanthanum-bromide ( $\text{LaBr}_3:\text{Ce}$ ) detectors. The  $B(E2; 2_1^+ \rightarrow 0_1^+)$  will give information on the evolution of ground-state collectivity approaching the predicted shape-transition region around  $N \approx 116$ . It is also expected that additional spectroscopic information on the low-spin states in  $^{182}\text{Hf}$  will be obtained in the experiment.

## Motivation

Neutron-rich refractory isotopes in the Hf – Pt region are predicted to undergo a phase transition from well-deformed prolate to oblate shapes with a critical neutron number of  $N \approx 116$  [1–3]. Figure 1 shows the evolution of the ratio of energies,  $E(4^+)/E(2^+)$ , and reduced transitions probabilities,  $B(E2; 2_1^+ \rightarrow 0_1^+)$ , for nuclei within this region. The  $E(4^+)/E(2^+)$  values suggest a well-deformed rotational behaviour in the known Hf isotopes but the W, Os, and Pt isotopes appear to evolve away from this limit and towards



**Figure 1:** Experimental (left)  $E(4^+)/E(2^+)$  and (right)  $B(E2; 2_1^+ \rightarrow 0_1^+)$  values in even- $A$  Hf, W, Os, and Pt isotopes. Values are taken from the Nuclear Data Sheets except the  $B(E2; 2_1^+ \rightarrow 0_1^+)$  for  $^{174}\text{Hf}$ ,  $^{176}\text{W}$  [9],  $^{178}\text{W}$  [10] and  $^{188}\text{W}$  [4].

that of a  $\gamma$ -soft rotor. Conversely, the  $B(E2; 2_1^+ \rightarrow 0_1^+)$  shows a relatively linear decrease as a function of neutron number for all isotopes as the shell closure at  $N = 126$  is approached.

The  $B(E2; 2_1^+ \rightarrow 0_1^+)$  reduced transition probability is an excellent probe of ground-state collectivity, with higher  $B(E2)$  values indicating more collective transitions. At present, the successful measurement of the half-life of the yrast  $2^+$  state in  $^{188}\text{W}$  in Bucharest [4] marks the only  $B(E2; 2_1^+ \rightarrow 0_1^+)$  measured for nuclei on the neutron-rich side of stability past the proton mid-shell ( $66 < Z < 82$ ). Thus, a precision measurement of the lifetime in  $^{182}\text{Hf}$  is desirable to further investigate changes in the collectivity in this transitional region. Based on the systematics of lighter Hf isotopes, a half-life of around 1.5 ns is expected for  $^{182}\text{Hf}$  – ideal for fast-timing measurement.

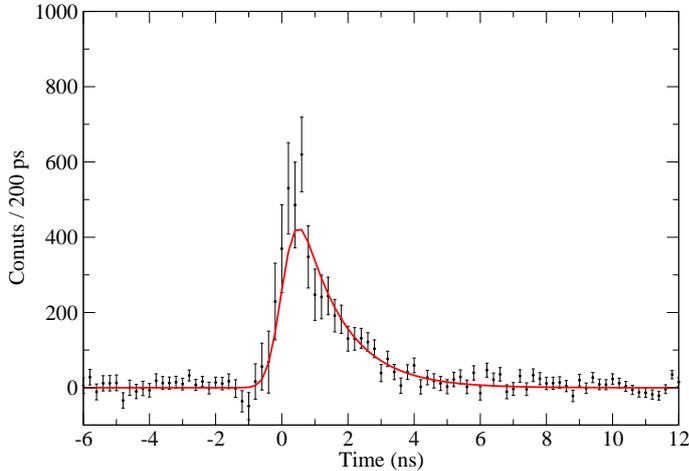
The measurement will also give an estimate of the deformation in this nucleus. The behaviour of  $^{182}\text{Hf}$  is expected to be close to the rigid rotor limit and so the simple rotational model of Bohr and Mottelsson [5] can be used to extract an estimate of the quadrupole deformation. This will be compared to existing theoretical predictions for deformation in this region (e.g. [2, 6]) along with new predictions to be performed for this experiment.

As the proposed  $^7\text{Li}$ -induced reaction gives significant population of low-spin, non-yrast states, it is also noted that the experiment is likely to give additional spectroscopic information on low-spin excited states in this nucleus. The second  $2^+$  state in  $^{182}\text{Hf}$  is only tentatively identified [7, 8] and little of the non-yrast structure has been established. The energy ratio of the yrast and second-excited  $2^+$  states is an important measurement in quantifying the degree of  $\gamma$ -softness of the nuclear shape.

## Experimental Details

We propose to measure the half-life of the yrast  $2^+$  state in  $^{182}\text{Hf}$  using in-beam fast timing with the ROSPHERE array of high-purity germanium (HPGe) and lanthanum-bromide

(LaBr<sub>3</sub>:Ce) detectors. <sup>182</sup>Hf will be populated using the <sup>180</sup>Hf(<sup>7</sup>Li, αp)<sup>182</sup>Hf incomplete-fusion/transfer reaction, with the <sup>7</sup>Li beam provided by the 9 MV Tandem van de Graaff accelerator. The feasibility of this reaction for in-beam fast-timing measurements has previously been demonstrated at Bucharest by the measurement of the yrast 2<sup>+</sup> state half-life in <sup>188</sup>W [4]. Figure 2 shows the final time spectrum obtained from this experiment.



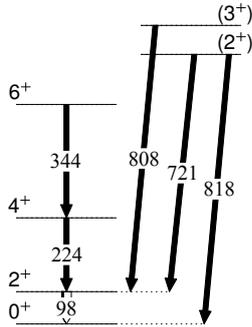
**Figure 2:** Time spectrum for the decay of the yrast 2<sup>+</sup> state in <sup>188</sup>W measured from the time difference between the 143-keV transition and all observed feeding transitions. The solid line represents a Gaussian-exponential convolution fit to the data giving a half-life of  $t_{1/2} = 0.89(13)$  ns.

A partial level scheme for <sup>182</sup>Hf relevant to this proposal is shown in Fig. 3. Ideally, the half-life of the yrast 2<sup>+</sup> state will be measured from the time difference between the full-energy photopeaks of the 4<sup>+</sup> → 2<sup>+</sup> (224-keV) and 2<sup>+</sup> → 0<sup>+</sup> (98-keV) transitions. A HPGe gate would be placed on the 6<sup>+</sup> → 4<sup>+</sup> (344-keV) transition to create a clean LaBr<sub>3</sub>:Ce  $E_{\gamma 1} - E_{\gamma 2} - \Delta T$  cube. However, due to the low cross-section for <sup>188</sup>W with the equivalent reaction, it was necessary to use a sum of HPGe gates on all feeding transitions and take the time difference between the 143-keV photopeak and a region of the LaBr<sub>3</sub>:Ce spectra from 250- to 750-keV. This continuous region contained the photopeaks and Compton-scattered  $\gamma$  rays of any transition feeding the yrast 2<sup>+</sup> state and higher lying states in <sup>188</sup>W. Though it is hoped that with the improved peak-to-total of the ROSPHERE, a time-difference spectrum using only full-energy photopeak gates can be created, it is likely that a similar procedure using a wide “start” gate will also be needed for <sup>182</sup>Hf.

## Rate Estimates and Beam-Time Request

In 10 days of beam time with a beam energy of 31 MeV and an average beam intensity of  $\sim 4$  particle-nA, a time spectrum (shown in Fig. 2) with  $\sim 2000$  counts was obtained for the yrast 2<sup>+</sup> state in <sup>188</sup>W. This required the sum of any direct and indirect feeding transitions with wide stop gates that included the Compton continuum of the spectrum. A significant proportion of these statistics were from feeding by non-yrast states in <sup>188</sup>W. The amount of non-yrast feeding is expected to be smaller for <sup>182</sup>Hf due to the more  $\gamma$ -rigid shape predicted for this nucleus, thus rate estimates for the proposed experiment are based on the yrast feeding only. Using only a single HPGe gate on the 6<sup>+</sup> → 4<sup>+</sup> transition in <sup>188</sup>W to generate the time spectrum yielded  $\sim 600$  counts (60 counts per day) but the

poor peak-to-total ratio made it impossible to accurately determine the half-life from this spectrum.



**Figure 3:** Partial level scheme of  $^{182}\text{Hf}$  [7]. The tentative spin and parity assignments are taken from Ref. [8] which suggests that they are the bandhead and first rotational state of the  $\gamma$  band.

The cross-section and spin input for this reaction is assumed to be approximately the same as that for the equivalent  $^7\text{Li} + ^{186}\text{W}$  reaction used to populate  $^{188}\text{W}$ . It was seen in the  $^7\text{Li} + ^{186}\text{W}$  reaction that increasing the beam energy from 31-MeV to 33-MeV increased the production cross-section and spin input for  $^{188}\text{W}$ . At 33-MeV, the coincidence rate between the  $6^+ \rightarrow 4^+$  and  $2^+ \rightarrow 0^+$  transitions in  $^{188}\text{W}$  was  $\sim 75\%$  greater than at 31-MeV. For this reason, a beam energy of 33-MeV is chosen to maximise population of  $^{182}\text{Hf}$ . However, the cross-section for the strongest fusion-evaporation channels was also increased by  $\sim 70\%$  with the higher beam energy and so the beam energy in the proposed experiment can be adjusted closer to the Coulomb barrier ( $\sim 29$  MeV) if contamination from fusion-evaporation reaction channels in the online spectra is large. In the previous experiment,  $^{188}\text{W}$  represented  $\lesssim 0.5\%$  of the total  $\gamma$ - $\gamma$  statistics obtained.

The new ROSPHERE array will improve the HPGe efficiency of the  $6^+ \rightarrow 4^+$  gate from  $\sim 1.4\%$  at 552-keV [11] with 8 HPGe detectors for  $^{188}\text{W}$  to  $\sim 2.1\%$  for the 344-keV transition [12] in  $^{182}\text{Hf}$ . The improved peak-to-total ratio due to the Compton-suppression of the ROSPHERE array should ensure that fewer counts are required in the final time spectrum to measure the half-life accurately. It is estimated that  $\geq 800$  counts will enable us to determine the half-life with better than 15% accuracy.

Assuming similar experimental conditions to the  $^{188}\text{W}$  experiment and taking into account the new HPGe efficiency and higher conversion coefficient for the  $2^+ \rightarrow 0^+$  ( $\alpha = 3.85$  for  $^{182}\text{Hf}$  [7],  $\alpha = 1.00$  for  $^{188}\text{W}$  [13]), we can expect to obtain  $\sim 70$  counts per day in a time difference spectrum utilising only a single gate on the  $6^+ \rightarrow 4^+$  transition in  $^{182}\text{Hf}$ . In 12 days of beam time we will obtain a minimum of  $\sim 800$  counts in the time difference spectrum, enough to measure the half-life of the yrast  $2^+$  state in  $^{182}\text{Hf}$  with a good degree of accuracy. **Thus we request 12 days of beam time.**

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